

**On the foundations of statistical mechanics: Extensivity of
the nonadditive entropy S_q , and generalized central limit
theorems**

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The (additive) Boltzmann-Gibbs-von Neumann-Shannon (BG) entropy is extensive in the thermodynamical sense for say classical short-range-interacting and other relatively standard systems. The situation is more subtle for complex systems such as quantum entangled ones, long-standing quasi stationary states in classical long-range-interacting Hamiltonian systems, optical lattices, plasma, among others. The nonadditive entropy S_q (S_1 being the BG entropy) appears to be extensive for a special value of the index q which differs from unity. This class of systems is discussed, as well as their connections to the Central Limit Theorem, which mathematically grounds BG statistical mechanics.

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